A new approach for estimating Titan’s electron conductivity based on data from relaxation probe sensors on the Huygens experiment

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A B S T R A C T

The Huygens Probe measured the electrical conductivity of Titan atmosphere from about 140 km down to the surface, employing relaxation and mutual impedance techniques. Previous analyses have shown some differences on the conductivity measurements obtained with two independent sensors—relaxation probe (RP) and mutual impedance probe (MIP). A 20-fold maximum discrepancy occurred around the conductivity peak at 60–70 km. To understand the nature of such discrepancy, we reassess the RP data by taking into account a geometrical factor related to the electrode finite size and the Debye length of the ionized medium. The present analysis implies replacing the standard Laplace field distribution by a more elaborated model considering the Poisson equation and the resistance between the RP electrodes and the medium. Although a complete understanding of the conductivity profile is still missing, this work brings RP and MIP data to a much better agreement. The conductivity maximum difference derived from the two sensors is now lower a factor of 2. This reassessment is also useful for future instruments and missions.

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1. Introduction

The Huygens Atmospheric Structure Instrument (HASI), one of the six instruments on board Huygens, was designed to characterize the physical properties of the lower atmosphere and surface of Titan, the planet-size moon of Saturn (Fulchignoni et al., 2005). During the descent of the Huygens Probe, the Permittivity Wave and Altimetry (PWA) subsystem searched for atmospheric permittivity and conductivity of Titan’s surface material, whose preliminary lower estimates are 2 and 4 × 10−10Sm−1, respectively (Grard et al., 2006).

In preparation for the descent of Huygens on Titan, the HASI subsystems were previously tested in the Earth atmosphere during several balloon campaigns using Huygens Probe mock-ups (López-Moreno et al., 2002). Conductivity measurements made in the Earth stratosphere during balloon flights were compatible with results reported by other teams, thus validating RP-PWA correct functionality. However, comparisons among RP and MIP measurements were not possible due to the absence of electrons in the terrestrial atmosphere at balloon altitudes. The latter instrument is sensitive to electrons only.

On Earth, various techniques can be used to measure electron conductivity in the atmosphere, namely Gerdien condenser, mutual impedance, and relaxation (Hale, 1984; Croskey et al,
the collected current from a non-linear system. The governing
equations for the fluid model, vacuum permittivity, Ne
to the Debye ratio, which is defined as
found an extreme sensitivity of the attracted current with respect
to the Debye ratio, which is defined as
They examined theoretically the operation of a spherical electro-
static probe in a weakly ionized, collision-dominated gas and
found an extreme sensitivity of the attracted current with respect
to the Debye ratio, which is defined as $D_2 = a/\lambda_D$, where $a$ is the electrode radius. The governing equations for the fluid model
describing the collected current form a non-linear system
comprising the continuity, flux, and Poisson equations for repelled
and attracted species (Su and Lam, 1963). Numerical simulations
are known to be extremely unstable because of the system of
equations high sensitivity with respect to initial conditions and
model parameterization. The work of Cicerone and Bowhill (1969)
was followed by Chang and Kodera (1985) and Godard and Chang
(1995), but their numerical results are too limited to be useful.
Huygens has provided evidence that the potential distribution
around the electrodes follows Poisson rather than Laplace
equation (López-Moreno et al., 2008). The probe was immersed in a
collisional, weakly ionized medium, where the fraction of
ionized molecules was always lower than $10^{-15}$, with a subsonic
turbulent velocity. Here we report a detailed analysis of electron
conductivity derived from the RP measurements onboard
Huygens and an associated numerical algorithm, which considers
geometrical effects related to the finite size of the electrode and
the Debye length of charged particles. RP sensors are widely
utilized for terrestrial (Holzworth, 1981; Rosen et al., 1982;
López-Moreno et al., 2001) and in planetary environments
measurements (Hamelin et al., 2006; López-Moreno et al.,
2008). Titan environment unique conditions allow us evaluating
the RP sensors performance, relaxation theory validity, and RP
and MIP comparative efficiency.

2. Electrical conductivity measurements techniques

The electrical conductivity sensors of the PWA subsystem were
integrated in two deployable booms, and consisted of two disks
(RP1, RP2) forming a double RP combined with four ring
electrodes (RX1, TX1, RX2, TX2) composing the MIP quadrupole.
Fig. 1 shows the arrangement of the electrodes in a deployed
configuration with respect to the gondola and a close view of one
boom holding the MIP and RP electrodes (Hamelin et al., 2007).
The booms are made of glass fiber insulating material; RP1 and
RP2 are mechanically similar. The connections run inside the
booms and comprise triaxial cables with the inner conductor
connected to the electrode. The intermediate conductor is actively
driven near the electrode potential and the outer connector is a
grounded shield. Additional, detailed information about PWA
architecture and boom configuration can be found elsewhere
(Fulchignoni et al., 2002; Hamelin et al., 2007).

PWA was operating from an altitude of 141 km down to the
surface, and during 32 min after landing. Part of the PWA data was
lost due to the failure of one of the transmission channels
between Huygens and the Cassini Orbiter (Lebreton et al., 2005).
This data loss reduces MIP time resolution by a factor of 2. The
RP1 data were lost and only the measurements performed with
RP2, the electrode designed for large conductivities, are available.

2.1. The mutual impedance probe

The conductivity of a homogeneous and isotropic medium can be
measured with an impedance probe. This instrument consists of
four electrodes comprising one transmitting dipole (TX1–TX2)
and one receiving dipole (RX1–RX2); the transmitting dipole is
fed by an AC current generator. The ratio of the potential
difference of the receiving electrodes to the injected current
yields the resistance of the medium, provided its homogeneity is
perturbed neither by the injected current nor by the dipole itself.
This situation is generally never encountered in electrolytes and
plasma because charged sheaths form around the electrodes.
Therefore, complementary studies were necessary to improve the
Titan MIP data. Additional laboratory tests were performed to
validate or improve the calibration results. Temperature effects
were included and numerical models of the MIP sensors and
electric circuitry have been developed to take into account the
proximity of the Huygens Probe body. The effect of the vertical
motion of the vessel in the ionized atmosphere is estimated in
both analytical and numerical ways (Hamelin et al., 2007).

The electron concentration is derived from combining the
conductivity measured by PWA with the neutrals density
and temperature (Fulchignoni et al., 2005). These quantities are
linked to the electron conductivity $\sigma_e$ as follows (Banks and
Kockarts, 1973):

$$\sigma_e = N_e \frac{q^2}{2.33 \times 10^{-14} N_0 T m_e},$$  

(1)
where \( m_e \) is the electron mass and \( N_n \) the neutrals number density. We have verified numerically, by running a turbulence model, that the neutrals number density, at the position of the MIP or the RP devices, is not affected by the shadowing effect of the vessel (Ibrahim, 2009). For example, Fig. 2 shows contour maps of the neutrals density \( n_n \) at three different altitudes: 130, 100, and 50 km. There is almost no difference between the upstream and the downstream regions of the vessel. Therefore, we have great confidence in MIP electron concentration estimates.

In the first part of the descent, above 110 km before the main parachute releasing, the MIP data are found inconsistent with a nominal response (Hamelin et al., 2007) and the passive ELF measurements are nearly similar to the noise level observed during the cruise phase (Simões et al., 2007). A probable explanation is that one or, less likely, both booms were not fully deployed during the mentioned period. Therefore, MIP data above 100 km were not analyzed. Table 1 shows the altitude profile of electron conductivity and derived electron concentration, and Debye ratio obtained by MIP, where the altitude is reported by Kazeminejad et al. (2007). The Debye ratio allows for a comparison between the electrode radius and the effective shielding length of a charged particle.

### 2.2. Relaxation probe—the Laplace approximation

The experimental set-up of the relaxation probe consists of an electrode exposed to the ionized medium that is biased at a negative or positive potential with respect to a reference level, the Huygens Probe structure. The electrode, a circular disk of radius \( a = 3.5 \text{ cm} \), is mounted on a boom at a distance of 15 cm from the

gondola. The sensor subsequently returns to its initial equilibrium potential by collecting positive or negative ambient charges. The sequence of measurements consists of four relaxation cycles of 56 s, where the source potential is successively set to +5, 0, −5, and 0 V. When the electrode is biased with respect to the reference potential, it collects a current produced by the attracted species. For atmospheric experiments, this current is produced by several terms: diffusion, convection, external electric field, and electrode potential gradient.

### Table 1

<table>
<thead>
<tr>
<th>Altitude (km)</th>
<th>( \sigma_e (\text{nS m}^{-1}) )</th>
<th>( N_e (\text{cm}^{-3}) )</th>
<th>( D_e )</th>
</tr>
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<tbody>
<tr>
<td>100</td>
<td>0.160</td>
<td>10.7</td>
<td>0.14</td>
</tr>
<tr>
<td>88.5</td>
<td>0.136</td>
<td>12.8</td>
<td>0.16</td>
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<td>78.9</td>
<td>0.056</td>
<td>12.4</td>
<td>0.16</td>
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<tr>
<td>78.7</td>
<td>0.251</td>
<td>31.2</td>
<td>0.26</td>
</tr>
<tr>
<td>70.9</td>
<td>1.81</td>
<td>283</td>
<td>0.84</td>
</tr>
<tr>
<td>70.8</td>
<td>2.14</td>
<td>335</td>
<td>0.92</td>
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<tr>
<td>62.9</td>
<td>3.00</td>
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<td>1.44</td>
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<tr>
<td>62.8</td>
<td>3.04</td>
<td>659</td>
<td>1.45</td>
</tr>
<tr>
<td>60.3</td>
<td>2.48</td>
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<tr>
<td>60.2</td>
<td>2.44</td>
<td>616</td>
<td>1.49</td>
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<tr>
<td>56.0</td>
<td>1.16</td>
<td>378</td>
<td>1.16</td>
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<td>55.9</td>
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<tr>
<td>42.3</td>
<td>0.284</td>
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<tr>
<td>42.3</td>
<td>0.181</td>
<td>133</td>
<td>0.07</td>
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The diffusion term is related to number density gradients close to the surface of the electrode in the undisturbed medium. It is driven by the thermal velocity of electrons, which is \( \approx 50 \text{ km s}^{-1} \). The convection term is related to the descent velocity of the system, of the order of a few \( 10 \text{ ms}^{-1} \). The electrode gradient term, about \( \approx 200 \text{ V m}^{-1} \) close to the electrode when charged at \( 5 \text{ V} \), produces an electron drift velocity much greater than a few \( \text{ km s}^{-1} \). As a result, convection can be neglected and the probe remains stationary with respect to the electronic fluid. The natural electric field also induces a small current. Grard et al. (2006) estimated an upper limit for the upward electric field \( E_z \approx 1 \text{ V m}^{-1} \), which is negligible compared to the electrode gradient term. Additionally, when the electrode is positively biased, all photo-electrons are returning back to the surface, and they should not contribute to the current. The electrode potential gradient is indeed the dominant term.

Assuming that the electrode is biased to a potential \( V \), the current is directly proportional to the electric potential gradient around the electrode. Then, for a conducting electrode, the medium is collisional, very weakly ionized, and the potential around the electrode can be described by the Laplace equation

\[
\nabla^2 V = 0,
\]

and the boundary conditions are

\[
V(r = a, t) = V_a(t)
\]

\[
V(r \to \infty, t) = 0,
\]

where \( V_a(t) \) is the electrode potential. Here, for the sake of simplicity and historical reasons, we assume that the electrode possesses spherical symmetry. If the electrode is a disk, such as on Huygens, we can apply a conformal map to switch from one geometry to the other. A conformal map is used to transform spherical into cylindrical geometries via the correction factor \( K \), which is 1 for a sphere and 2/\( \pi \) for a disk. Therefore, we shall consider a spherical geometry, which corresponds to a one-dimensional solution, rather than a disk geometry, a more complex two-dimensional numerical problem.

For a spherical electrode embedded in an homogeneous medium, the concentration of attracted particles \( N_a(r = a, t) \) is always equal to the undisturbed charge concentration \( N_0(r = a, t) = N_0 \). In this case, the inward current \( I_r \) is given by (Mozer and Serlin, 1969; Kellog and Weed, 1969; Godard, 2007)

\[
I_r(t) = 4\pi K a^2 \sigma_a \left[ \frac{dV_a(t)}{dr} \right]_{r=a}, \quad V_a(t) = V_a(t) \frac{a}{r}
\]

where \( \sigma_a \) is the electric conductivity for attracted species, \( \frac{dV}{dr} \) the electric field strength on the electrode surface, \( r \) the radial distance, and \( R_e \) the effective resistance of the electrode in the ionized medium.

On the other hand, the RP theory is also directly linked to the theory of electrostatic probes in a slightly ionized, collision-dominated gas where an electrode or any object acts as a particle sink with \( N_0(r = a, t) = N_0 \) at the electrode surface (Cicerone and Bowhill, 1969; Swift and Schwarz, 1969; Godard, 2007). In particular, Swift and Schwarz (1969, pp. 177–181) commented in detail the derivation of the boundary condition \( N_a(r = a, t) = 0 \) and the influence of the mean free path. It is clear that exact boundary conditions in any model involving differential equations are directly linked to the well-posedness of the problem. If the RP potential is zero, the only electron or ion density perturbations in the electrode vicinity would be due to diffusion, convection, and to the geometry of the electrode itself. In the case of Huygens, we verified that convection dominates. Therefore, results for the neutral flow could reasonably be extended to electrons or ions (Ibrahim, 2009). This means the electron density would be uniform around the vessel, provided that it was at zero potential; we can then assume \( N_e(q_0, t) = N_e(r \to \infty, t) \), where \( q_0 \) would be the equivalent vessel radius. Since the RP disk is small and roughly oriented in the direction of the flow, the diffusion and convection currents are similar when a zero electrode potential applies. We have verified that for a Laplace model, because of its linearity, the collection of current, and consequently the RP potential decay, is independent of the electron concentration boundary condition at the electrode surface. In fact, if we choose \( N_0(r = a, t) = \pm N_e(r \to \infty, t) \), where \( a \) is in the range \( 0 \leq a \leq 1 \), almost identical results are obtained. Because this work is focusing on the data processing rather than in new developments of mathematical models for RP, we shall omit a lengthy demonstration of the above result. However, this important result is not true for a Poisson field, which corresponds to a non-linear model (Godard et al., 2010).

Let us now consider the signal from the RP sensor. For a Laplace potential, the Debye ratio is equal to zero, and the free space capacitance around the electrode is constant. For a disk or a sphere simplified model, we find

\[
\frac{\sigma_a}{\varepsilon_0} = \frac{1}{K_a C_e},
\]

where \( C_e \) is the electrode capacitance.

If the reference potential is stable, the potential difference between the RP electrode and the Huygens vessel follows the exponential law

\[
V_a(t) = (V_0 - \Delta V_f) e^{-t/\tau} + \Delta V_f,
\]

where \( V_0 \) and \( \Delta V_f \) are the initial and floating potentials, respectively. The slope of the potential decay, or time constant \( \tau \), is related to the resistance and capacitance of the electrode in the plasma by \( \tau = R_e C_e \) and provides the polar components of the electrical conductivity

\[
\frac{\sigma_a}{\varepsilon_0} = \frac{\delta_0}{\tau}.
\]

In order to reduce the speed of decay of the electrode potential for a given conductivity, thus extending the range of measurements towards larger conductivities, a discrete capacitor \( C_a = 352.5 \text{ pF} \) was connected in parallel with the RP2 sensor. Under these conditions, the global capacitance is replaced by \( C_a + C_e \), and the time constant becomes

\[
\tau = R_0(C_a + C_e) = \frac{C_a + C_e}{\sigma_a} \frac{\varepsilon_0}{\sigma_a}.
\]

At this stage, and we would like to emphasize it again, this classical model of RP gives, in some cases, a 20-fold discrepancy with respect to MIP results.

2.3. Relaxation probe—the Poisson approximation

If the size of the electrode is comparable to the Debye length, the resistance and the capacitance of the system RP-medium are modified, and they are functions of the applied potential. In order to consider a reasonable computational approach, let us consider a quasi-static approximation for a slowly time varying problem. Assuming an instant stationary solution, it is easier to compute the electrode current for a given potential. Therefore, we can build a set of I–V characteristic functions and compute the resistance vs. potential or time by interpolation, it is possible building a continuous set of resistances and capacitances for various Debye ratios. Now we replace (2) by Poisson equation

\[
\nabla^2 V = -\frac{q_0}{\varepsilon_0}(N_+ - N_-),
\]
where \( N_+ \) and \( N_- \) are the concentration of positive and negative charges (mainly electrons in the case of Huygens), respectively. To solve Eq. (11) it is necessary to compute, simultaneously, the basic fluid equations
\[
\Gamma_\pm = -D_\pm \nabla N_\pm = \mu_\pm N_\pm \nabla \phi,
\]
\[
\nabla \cdot \Gamma_\pm = 0,
\]
where \( \mu_\pm \) and \( D_\pm \) are the mobility and diffusion coefficients, respectively, and \( \Gamma \) is the particle flux number density. The flux equations are linked to the boundary conditions
\[
N_\pm (r = a) = 0
\]
\[
\lim_{r \to \infty} N_\pm (r) = N_\infty.
\]

For the sake of simplicity, and to keep the same notation used by Cicerone and Bowhill, we consider \( N_- = N_0 \). The classical boundary conditions at the electrode surface are known from collisional electrostatic probe theory. We refer to Swift and Schwar (1969) for a derivation as a function of pressure. A review of the theories governing the collection of charges by biased probes and the numerical solution for several values of the relevant parameters can be found in Cicerone and Bowhill (1969). They suggested power-law fits for the I–V characteristics. Results are presented as a function of dimensionless potential \( \phi \), defined as the ratio of the electric potential energy with respect to the thermal energy \( \phi = V_0 q_e / (k_B T) \), for a Debye ratio in the range \( 0.1 < D_\lambda < 1 \). For the Huygens conditions, it is necessary to interpolate and extrapolate the results. Fig. 3 shows the dimensionless current as a function of the Debye ratio for \( \phi = 500 \). We observe that the values follow a linear correlation in a double logarithm scale. From physical considerations and perturbation theory, the derivative of the current with respect to the potential \( \phi \) is zero, and the potential \( \phi \) is a linear relation is not valid. For low \( D_\lambda \), in the range \( 0 < D_\lambda < 0.1 \), we have obtained the dimensionless inward electron current considering Hermite interpolation. Fig. 4 shows the normalized dimensionless inward current with respect to the diffusion value \( 4 \pi a N_0 q_e D_\lambda = 4 \pi a N_0 q_e / q_e = D_\lambda \phi = \mu_+ k_B T/q_e \) as a function of \( |\phi| \) for various Debye ratios. The diffusion value corresponds to the case where the electrode potential is zero, and the diffusion current is only due to electron concentration gradients. Here we assume that the Einstein relation for diffusion, \( D_\lambda = \mu_+ k_B T/q_e \), is valid, and the data from Hasted (1964) suggest that it should be aborderline case; \( \mu_+ \) is the electron mobility. We observe the classical decrease of the inward current density as the Debye ratio increases and a slow variation of the current for large values of \( D_\lambda \). The current seems to saturate for \( D_\lambda > 4 \). For a more accurate RP data processing, it is necessary to take into account the fact that the resistance and capacitance of the electrode are functions of the electrode potential and Debye ratio.

Because of the supplementary capacitance \( C_u \), which is much higher than the electrode capacitance, the data processing for Huygens RP sensors does not require the computation of the electrode capacitance in the ionized medium. Even if the calculation of \( C_u \) is unnecessary, we have obtained a first order computation of the capacitance of the electrode-plasma system (see Godard, 2007 for details). Fig. 5 shows the dimensionless spherical electrode capacitances with respect to values in vacuum, for various values of the Debye ratio. We observe a slow decay of capacitances for large potentials. In the limit of a zero Debye length, and for large attracting potentials, the capacitance approaches the solution in vacuum.
Considering Figs. 4 and 5, it is possible to simulate a relaxation signal with different input parameters, namely descent velocity, negative ion conductivity, or the reference potential.

The theoretical potential signal $V_{th}$ between the RP electrode and the medium satisfies the following equation

$$I = \frac{dQ}{dt} = \frac{d}{dt}(CV_{th}) = -\frac{V_{th}}{R}$$  \hspace{1cm} (14)

where $I$ is the collected current and $Q$ is the charge of the electrode; the RP signal is then written

$$\frac{dV_{th}}{dt} = \frac{V_{th}}{RC} - \frac{V_{th}}{C} \frac{dC}{dV_{th}} \frac{dV_{th}}{dt}$$

where $j$ is the iteration index and $h$ the time step.

First, the signal is simulated numerically with a guessed electron concentration. Then, results from Fig. 4 are input parameters for the calculation of the resistance. These outputs are then used to solve Eq. (16). Finally, the electric conductivity is adjusted by calculating the minimum of the residual function, $\mathcal{R}$, defined as the sum of the least absolute deviations according to

$$\min(\mathcal{R}(\sigma_e)) = \frac{1}{n} \sum_{i=1}^{n} |V_{th}(t_i, \sigma_e, D) - V_{\text{meas}}(t_i)|,$$  \hspace{1cm} (17)

where $n$ is the number of observations and $V_{\text{meas}}(t_i)$ the experimental data. The inferred conductivity is then found by residual minimization. We find Eq. (17) an appropriate method because it reduces the weight of large residuals. Fig. 6 shows an example of the residual $\mathcal{R}$ as a function of the electron conductivity obtained at an altitude of $\approx 63$ km. This minimization function is unimodal, and forms a cusp near the global minimum.
minimum. We have performed a straightforward one variable half interval search.

3. Results and discussion

Fig. 7 shows six relaxation cycles obtained when electrons are attracted, \( V_0 = 5 \text{V} \); the fitting lines are computed by solving Poisson equation. We observe very good fits between experimental and simulated data. Table 2 shows the altitude and electron conductivity for each relaxation cycle of Fig. 7. The electron conductivity obtained by MIP is also shown for comparison (Hamelin et al., 2007). The conductivity derived from RP, including our minimization technique for a Poisson field, agrees reasonably well with the measurements provided by MIP. We have also observed that the electron conductivity obtained by means of minimization algorithm, Eq. (17), is very sensitive to the collected electron current. At this stage, we do not know if the difference originates from MIP or RP analysis. We do not question the scientific validity of Cicerone and Bowhill work, because their results coincide with those obtained by other algorithms. However, it is possible that our interpolation/extrapolation scheme introduces additional errors, especially at small Debye ratios. For the sake of comparison, the conductivity obtained by assuming a Laplace field at the peak is about 20 times lower than that provided by the MIP sensor.

Table 3 shows the electron concentration, electron conductivity, and Debye ratio for all the relaxation cycles. Note that the ambient electron concentration is not necessarily accurate close to the electrode, and we may have a more complex relationship at the vicinity of the electrode with possible shadowing effects from the gondola, especially if the boom was not completely deployed above 110 km as proposed by Hamelin et al. (2007). We observe very small Debye ratios at high altitudes, from 134 km down to 70 km; below these altitudes, the Debye ratio is larger. We found similar patterns from MIP results. From the electron concentration profiles shown in Fig. 8, we find that MIP and RP measurements follow a similar pattern.

4. Conclusions

Because two independent techniques are used to investigate the atmospheric conductivity during the descent of the Huygens Probe on Titan, comparison between RP and MIP measurements is possible. The measurements obtained by the RP sensor on Huygens indicate a geometrical effect related to the ratio of the size of the electrode to the Debye length of charged particles. Using a similar approach to that of Cicerone and Bowhill and a conformal mapping of a sphere into a disk, we are able to reduce the difference between MIP and RP results from a factor of 20 to roughly a factor of 2. To understand whether a better agreement between RP and MIP measurements is possible, it is our intention to keep refining the conductivity retrieval method with a more elaborated numerical simulation that also includes shadowing effects between the gondola and the RP sensor.

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References


